
Mlindex

Bayes

$$f(x|a, \lambda) = \lambda a^\lambda x^{\lambda-1}, \quad x \in [0, a]$$
$$F(x|a, \lambda) = 1 - a^\lambda x^{\lambda-1}, \quad x \in [0, a]$$

$a \lambda$

$a \lambda$

$RP a \lambda$

$\theta \lambda$

$$L \lambda \theta \omega \left[\left(\frac{\theta}{\lambda} \right)^c c \frac{\theta}{\lambda} \right] \omega c$$

c

c

c

$X \quad X \quad X \quad X_n \quad X_n \quad RP a \lambda$
 $x \quad x \quad x_n$

$a \lambda$
 $RP a \lambda \quad a \quad \lambda$

$$\lambda_{MLE} = n \binom{n}{i} \frac{a_{MLE}}{x_i}$$
$$a_{MLE} = \{x_i\} x_n$$

$$\begin{aligned}
 & \lambda_{MAP} \frac{n \beta}{\gamma t} \\
 & t \prod_i^n x_i \sim a \Gamma(\beta \gamma) \beta \gamma \quad \beta \gamma \\
 & X \sim X_n \sim \lambda \quad \Gamma(\beta \gamma) \quad \beta \gamma \quad \beta \gamma \quad p \sim X | \lambda \\
 & \pi(\lambda) = \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^\beta e^{-\gamma \lambda} \\
 & p \sim X | \lambda \sim \prod_i^n \lambda a^\lambda x_i^\lambda \sim \lambda^n a^{n \lambda} \prod_i^n (x_i^\lambda) \sim \frac{\lambda^n}{\prod_i^n x_i} e^{-\lambda t} \prod_i^n x_i \sim a \\
 & p \sim X | \lambda \sim \pi(\lambda) \sim \frac{\lambda^n}{\prod_i^n x_i} e^{-\lambda t} \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^\beta e^{-\gamma \lambda} \sim \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^{n+\beta} e^{-\gamma t - \lambda} \\
 & \lambda \sim p \sim X | \lambda \sim \pi(\lambda) \sim \lambda^{n+\beta} e^{-\gamma t - \lambda} \quad p \sim X | \lambda \sim \pi(\lambda) \sim \lambda \\
 & g \sim \lambda \sim \lambda^{n+\beta} e^{-\gamma t - \lambda} \quad g \sim \lambda \quad g \sim \lambda \quad g \sim \lambda \\
 & (g \sim \lambda)' \sim \frac{n \beta}{\lambda} \gamma t \\
 & \lambda \\
 & \lambda_{MAP} \frac{n \beta}{\gamma t} \\
 & \lambda \\
 & \lambda \\
 & a \quad \lambda \\
 & X \sim X \sim X_n \sim RP \sim a \sim \lambda \quad a \sim \lambda \\
 & X \sim X \sim X_n \sim x \sim x \sim x_n \\
 & \pi
 \end{aligned}$$

$$\int_0^{\infty} p(X|\lambda) \pi(\lambda) \lambda \left[\int_0^{\infty} \omega \left[\left(\frac{\lambda X}{\lambda} \right)^c - \frac{\lambda X}{\lambda} \right] p(X|\lambda) \pi(\lambda) d\lambda \right]$$

$$\lambda X \quad X \quad X \quad X \quad X_n$$

$$\begin{aligned}
 & \lambda_B(X) = (E(\lambda|X))^{-c} \left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c \\
 & \Gamma(\beta, \gamma) = \lambda^{-\beta} \pi(\lambda) \\
 & \pi(\lambda) = \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^{\beta-1} e^{-\gamma\lambda} \\
 & f(x|\lambda) = \lambda a^\lambda x^{a-1} e^{-\lambda x} \\
 & L(X|\lambda) = \prod_{i=1}^n \lambda a^\lambda x_i^{a-1} e^{-\lambda x_i} = \lambda^n a^{n\lambda} \left(\prod_{i=1}^n x_i^{a-1} \right) e^{-\lambda \sum_{i=1}^n x_i} \\
 & \pi(\lambda|X) = \frac{L(X|\lambda) \pi(\lambda)}{\int_0^\infty L(X|\lambda) \pi(\lambda) d\lambda} \\
 & \quad = \frac{\frac{\lambda^n}{\prod_{i=1}^n x_i} e^{-\lambda \sum_{i=1}^n x_i} \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^{\beta-1} e^{-\gamma\lambda}}{\int_0^\infty \frac{\lambda^n}{\prod_{i=1}^n x_i} e^{-\lambda \sum_{i=1}^n x_i} \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^{\beta-1} e^{-\gamma\lambda} d\lambda} = \frac{\gamma^\beta}{\Gamma(\beta)^n \prod_{i=1}^n x_i} \lambda^{n+\beta-1} e^{-\gamma\lambda} \\
 & \quad = \frac{\lambda^{n+\beta-1} \int_0^\infty \gamma^\beta e^{-\gamma\lambda} d\lambda}{\Gamma(\beta)^n \prod_{i=1}^n x_i}
 \end{aligned}$$

$$\lambda_{EB} \int_D \lambda_B(a,b) f(a,b) da db$$

$$\lambda \int_D \lambda_B(a,b) f(a,b) da db \quad D \quad a \quad b \quad f(a,b) \quad a$$

$$b \quad D \quad \lambda_B(a,b) \quad \lambda$$

$$\lambda_{EB} \int_D \lambda_B(a,b) f(a,b) da db \quad E[\lambda_B(a,b)]$$

$$\lambda \quad \lambda_B(a,b) \quad a \quad b \quad \lambda \quad \lambda$$

$$\Gamma(\beta, \gamma) \quad X \quad X \quad X_n \quad RP \quad a \quad \lambda \quad a \quad \lambda$$

$$x \quad x \quad x_n \quad \lambda \quad \pi \quad \lambda \quad \beta \quad \gamma \quad \beta \quad \gamma \quad X \quad X \quad X \quad X_n$$

$$\lambda_{EB}(X) \quad \frac{m}{m} \quad \frac{m}{t} \quad \left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c d\beta$$

$$t \quad \begin{matrix} n \\ i \end{matrix} \quad x_i \quad a \quad \Gamma(\beta, \gamma) \quad \beta \quad \gamma \quad U(\quad) \quad U(\quad m)$$

$$RP \quad a \quad \lambda \quad \lambda$$

$$\lambda_B(X) \quad \frac{\left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c}{\gamma \quad t}$$

$$t \quad \begin{matrix} n \\ i \end{matrix} \quad x_i \quad a \quad \lambda \quad \Gamma(\beta, \gamma) \quad \beta \quad \gamma \quad \beta \quad \gamma \quad \beta \quad \gamma$$

$$\beta \quad \gamma \quad U(\quad) \quad U(\quad m) \quad f(\beta, \gamma) \quad \frac{1}{m}$$

$$RP \quad a \quad \lambda \quad \lambda$$

$$\lambda_{EB}(X) \quad E(\theta|X) \quad \frac{\left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c}{\gamma \quad t} \int f(\beta, \gamma) d\beta d\gamma$$

$$\frac{\left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c}{\gamma \quad t} \frac{1}{m} d\beta d\gamma$$

$$\frac{1}{m} \left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c d\beta \quad \frac{1}{\gamma \quad t} d\gamma$$

$$\frac{1}{m} \quad \frac{m}{t} \quad \left(\frac{\Gamma(n, \beta)}{\Gamma(n, \beta, c)} \right)^c d\beta$$

$$\lambda \quad \Gamma(\beta, \gamma) \quad \pi(\lambda) \quad \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^\beta \quad e^{-\gamma\lambda} \quad \beta \quad \alpha$$

$$\pi(\lambda) \int_0^a \int_0^\lambda \frac{\gamma^\beta}{\Gamma(\beta)} \lambda^\beta e^{-\gamma\lambda} d\beta d\gamma \pi(\lambda)$$

$$\lambda_{HB} = \frac{\int_0^a \int_0^\lambda \frac{\gamma^\beta \Gamma(n-\beta)}{\Gamma(\beta) \gamma t^{n-\beta}} d\beta d\gamma}{\int_0^a \int_0^\lambda \frac{\gamma^\beta \Gamma(n-\beta)}{\Gamma(\beta) \gamma t^{n-\beta}} d\beta d\gamma}$$

$$t \prod_{i=1}^n x_i \sim a \Gamma(\beta\gamma) \beta \gamma U(\cdot) U(m)$$

$$X \sim X_n \sim RP \sim a \lambda \sim a$$

$$L \sim \prod_{i=1}^n \lambda a^\lambda x_i^\lambda \sim \lambda^n a^{n\lambda}$$

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$Var\ X$ $X\ X\ X\ X$ $E\ X$

$$E\ X = \frac{\lambda a}{\lambda}$$

$$Var\ X = \frac{\lambda a}{\lambda} - \left(\frac{\lambda a}{\lambda}\right)^2$$

$$= a - a^2$$

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Mlincx

Bayes

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**Bayes Estimates of Shape Parameters of Reverse Pareto Distribution
under Mlinex Loss Function**

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Abstract